

# The Various Variations of Cool Stars

Variations of Solar-like Dwarfs  
(luminosity class V) on a Veritably  
Vertiginous Variety of Timescales

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(with special thanks to the organizers, Afrin<sup>®</sup>, Sudafed<sup>®</sup> for making this talk possible)

# Variability in Cool Dwarfs

Present on many temporal and spatial scales

Of fundamental importance for characterizing/ understanding MHD flows, dynamos, energetics, etc.... everything interesting!

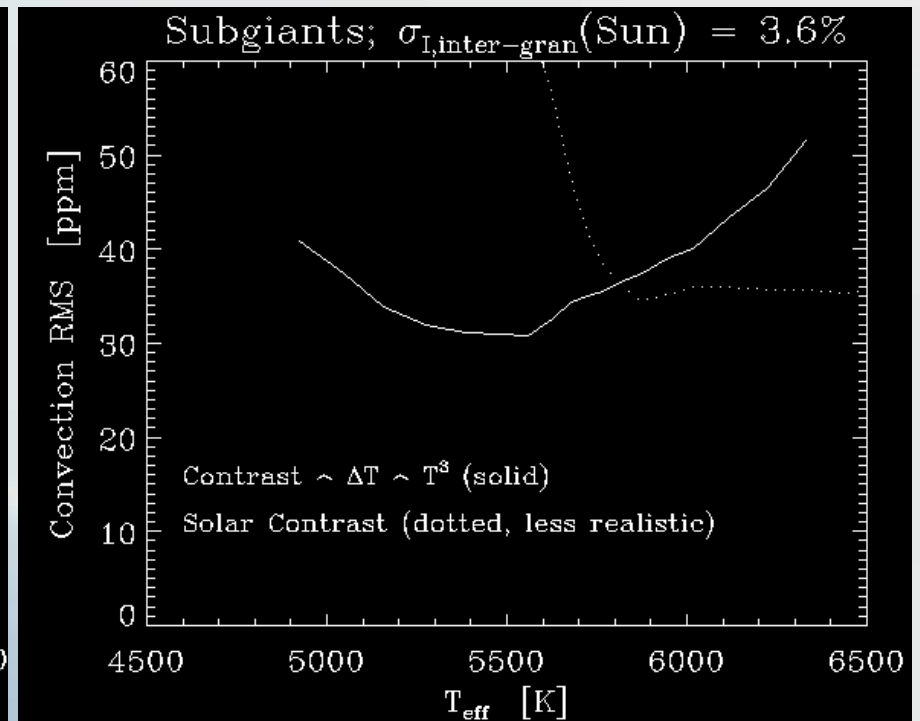
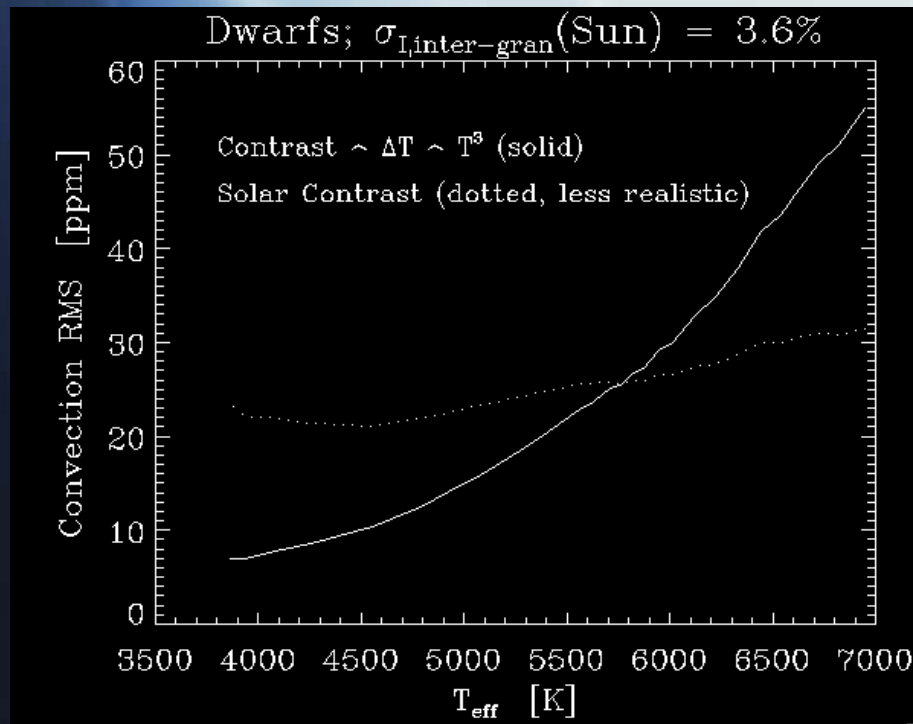
## Phenomena/Timescales:

- Convection [mins]
- Flares [mins-hours]
- Rotation [hours-weeks]
- Differential rotation [weeks-months]
- Active Region growth/decay [weeks-months]
- Active Longitude switching (“flip-flops”) [years]
- Activity cycles [years-decades]
- Long-term maxima/minima (eg, Maunder min.) [centuries]

# Convection

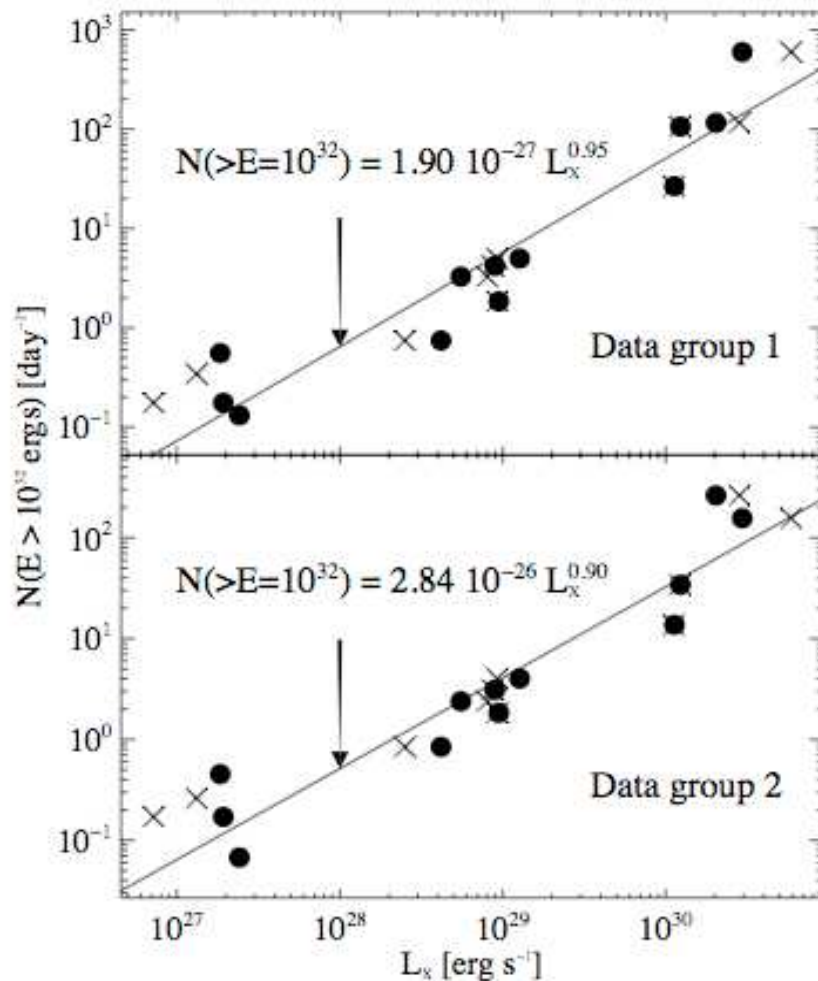
(Limited) info from models, line bisectors

- Assume cell size scales as pressure scale height:  $d \sim (H_p / H_{p,Sun}) d_{Sun}$
- Assume intensity RMS goes as
$$\sigma_{I,cell} \sim (\Delta F / \Delta F_{Sun}) \sigma_{I,cell,Sun} \sim (T_{eff} / T_{eff,Sun})^3 \sigma_{I,cell,Sun}$$
 (here, used  $\sigma_{I,cell,Sun} = 3.6\%$ )
- Number of cells  $N \sim (R_*/d)^2$
- Expected stellar RMS intensity is then  $\sigma_I \sim N^{1/2} \sigma_{I,cell}$
- Noise floor for Kepler/Corot-type planet transit/helioseismology missions



# Flares

Best data for GK stars probably from X-ray monitoring  
(optical data only sees brightest flares on faintest stars)

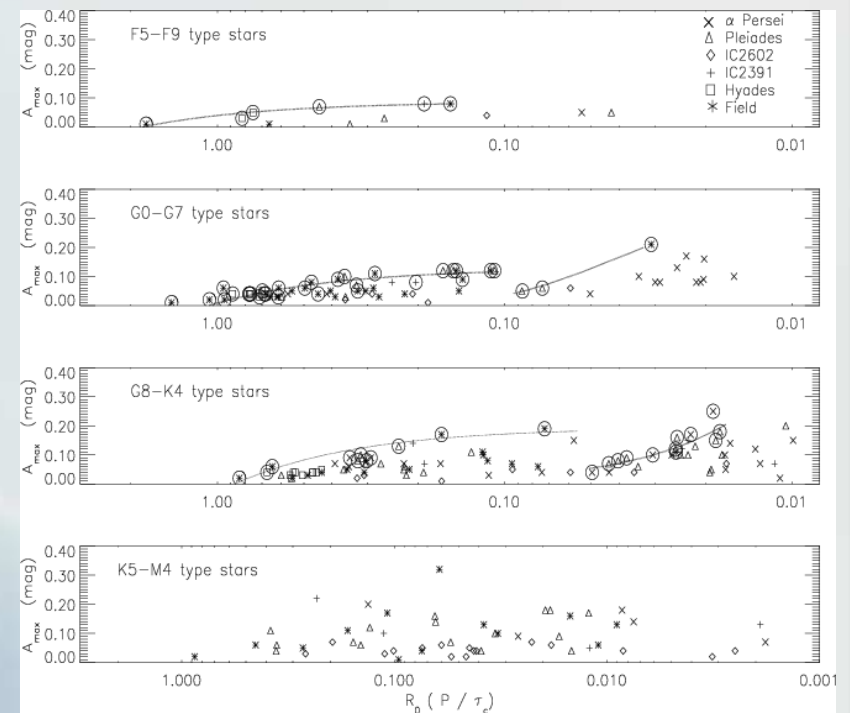
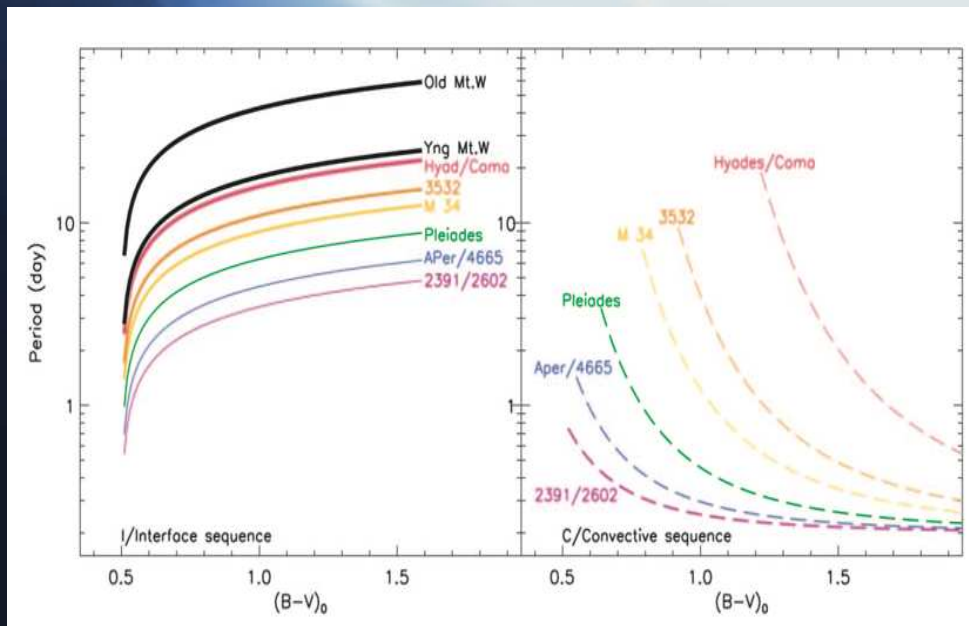


- $N(E > 10^{32} \text{ ergs}) \sim L_X^{0.9}$  (Audard et al 2000)  $\sim$  an X1 flare
- $dN/dE \sim E_{\text{tot}}^{(1-\alpha)}$ ;  $\alpha_{\text{Sun}} \sim 1.6$ ,  
 $\alpha_{\text{youngSun}} \sim 2.2$  (Audard et al 2000)
- $L_X \sim t^{-0.6}$  (Güdel et al 1998);  $\alpha \sim L_X^{0.2}$  (fit to Audard et al 2000)
- Can use to extrapolate to other E ranges, estimate number of X-ray, white light flares for Sun at any age.

# Rotation

Data: photometry (spot+plage), activity diagnostic (Ca II, Xray), line profile shape, Doppler imaging

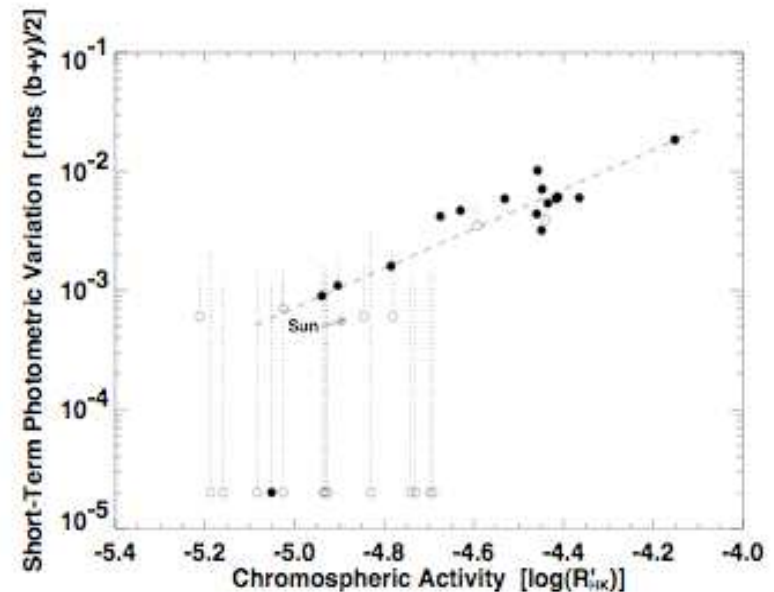
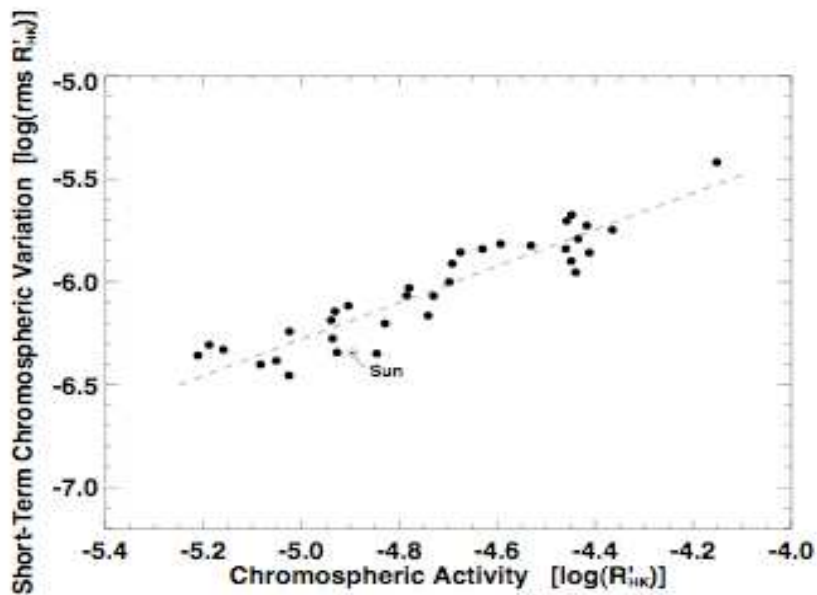
- Rotation spans 0.2 - 50+ d in single dwarfs
- $P_{\text{rot}} \sim f(M)t^{0.55}$  (Skumanich 1972; Barnes 2003, “I” branch = **interface** dynamos?)
- $P_{\text{rot}} \sim \exp(-g(M,t)t)$  (Barnes 2003, “C” branch = **convective** dynamos?)
- Maximum amplitude  $A_{\text{pho}}(\text{max}) \sim a - b(P_{\text{rot}}/\tau)$  (Messina et al 2001)  
(spread below this due to sini, distribution of spots); increases for **lower mass**



# Rotation II. RMS variation

Data: intra-seasonal HK, photometric RMS (includes differential rotation, AR growth/decay)

- $\sigma_{\text{HK}}(\text{short-term}) \sim (F'_{\text{HK}}/F_{\text{bol}})^{0.88}$  (using Radick et al 1998)
- $\sigma_{\text{pho}}(\text{short-term}) \sim (F'_{\text{HK}}/F_{\text{bol}})^{1.62}$  (using Radick et al 1998)
- So  $\sigma_{\text{pho}}(\text{short-term}) \sim \sigma_{\text{HK}}(\text{short-term})^{1.84}$

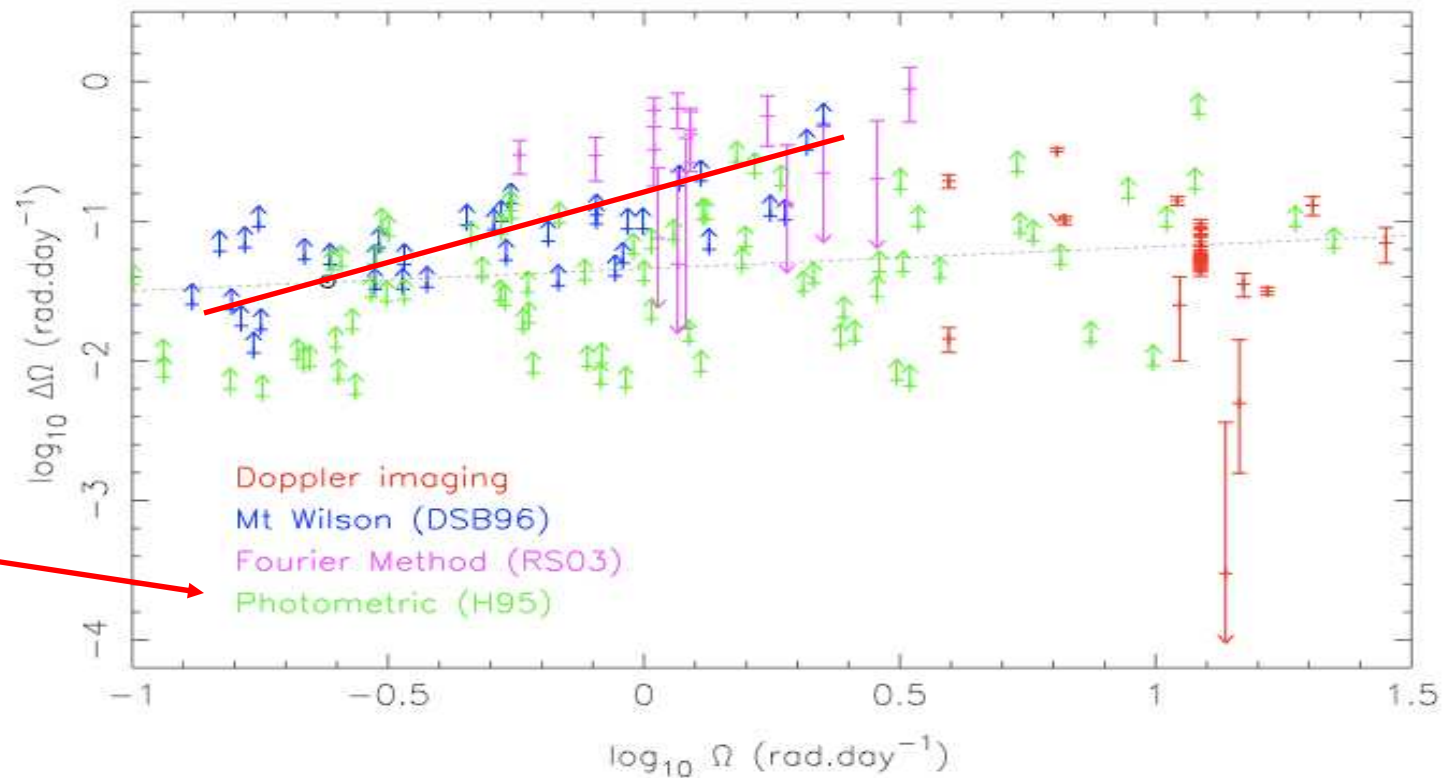


# Differential Rotation

Data: focus on single dwarfs, similar kinds of data, get  $\Delta P_{\text{rot}}$

- Barnes et al 2005 found  $\Delta\Omega \sim \Omega^{0.1}$  (!), but included evolved stars & binaries (Hall 1995)
- $\Delta\Omega \sim \Omega^{0.7}$ ,  $\Delta P_{\text{rot}} \sim P_{\text{rot}}^{1.3}$  (Donahue et al 1996) ( $P_{\text{rot}} > 3\text{d}$ ) [other dwarf data consistent]
- $\Delta\Omega$  saturation, decline for  $P_{\text{rot}} < 3\text{d}$ ? (Barnes et al 2005, reinterpreted)
- $T_{\text{eff}}$ , Mass dependence for high  $\Omega$  (Barnes et al 2005)

Many evolved stars & binaries



# Active Region Growth/Decay

Data: Ca II HK, photometry

Analyze: spot lifetimes, pooled HK variance ( $\int \sigma_{HK}^2$ )

active  $P_{rot} \sim 8d$     inactive  $P_{rot} \sim 20d$

Jumps in  $\int \sigma_{HK}^2$  at significant new phenomena:

rotation, →

ARGD, →

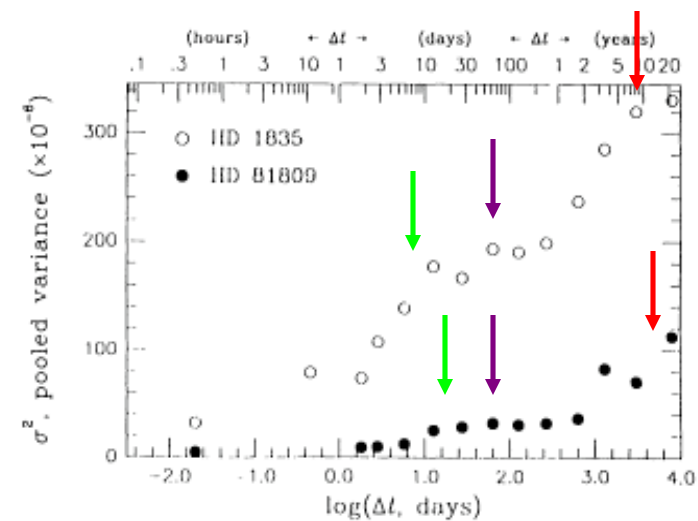
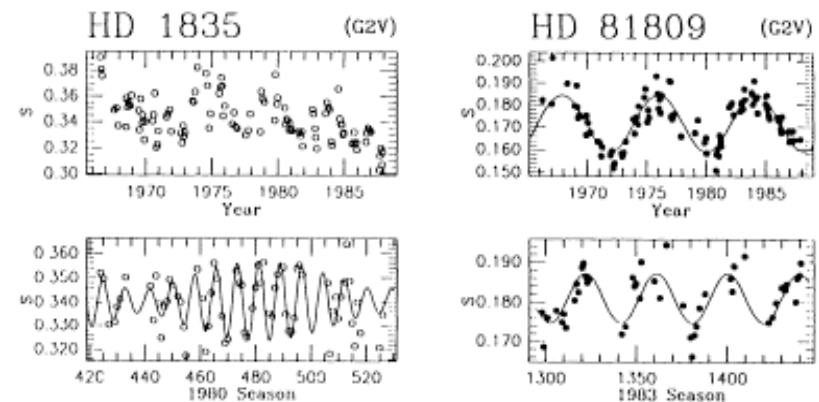
cycles, →

Long-term

Rotation

ARGD

Pooled variance  $\int \sigma_{HK}^2$



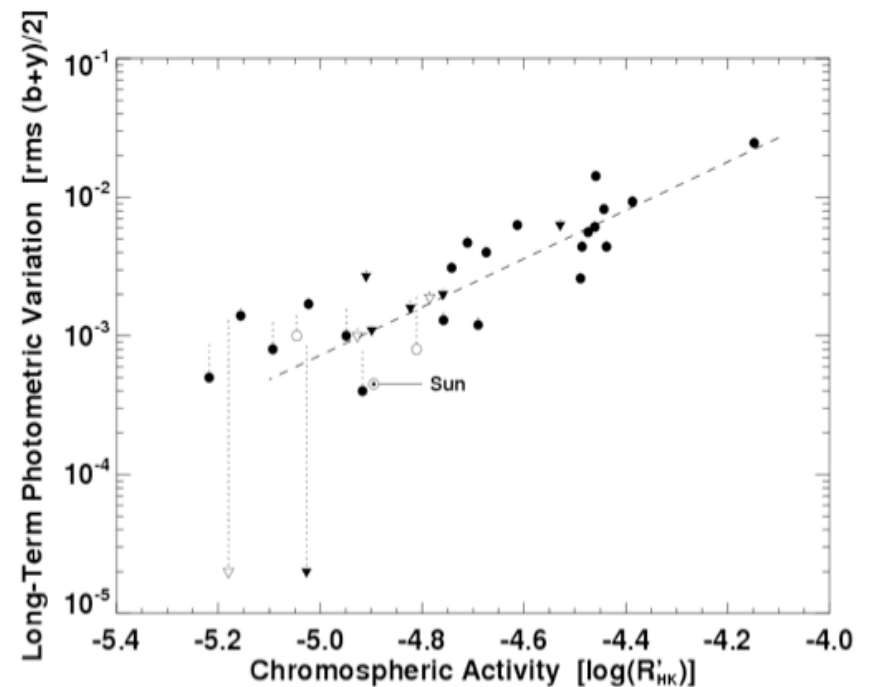
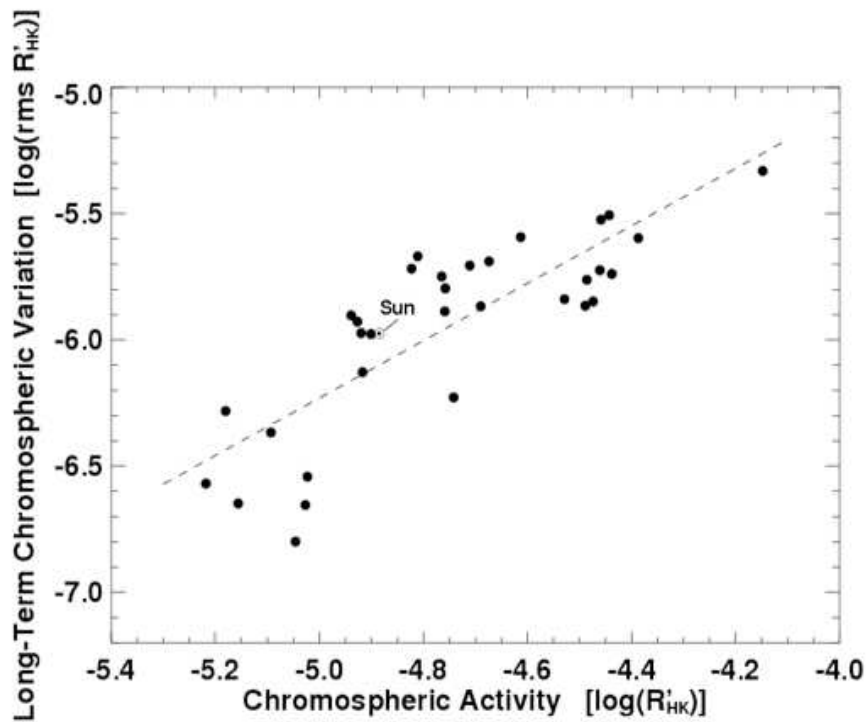
Dobson et al 1990



# Magnetic Cycles. RMS variation

Data: seasonally averaged HK, photometric RMS (includes active longitude flip-flops, some AR growth/decay)

- $\sigma_{\text{HK}}(\text{long-term}) \sim (F'_{\text{HK}}/F_{\text{bol}})^{1.15}$  (using Lockwood et al 2007)
- $\sigma_{\text{pho}}(\text{long-term}) \sim (F'_{\text{HK}}/F_{\text{bol}})^{1.85}$  (using Lockwood et al 2007)
- So  $\sigma_{\text{pho}}(\text{long-term}) \sim \sigma_{\text{HK}}(\text{long-term})^{1.61}$
- And:  $\sigma_{\text{pho}}(\text{long-term}) \sim \sigma_{\text{pho}}(\text{short-term})^{1.14}$  ;  $\sigma_{\text{HK}}(\text{long-term}) \sim \sigma_{\text{HK}}(\text{short-term})^{1.31}$



# Magnetic Cycles II. Cycle Period

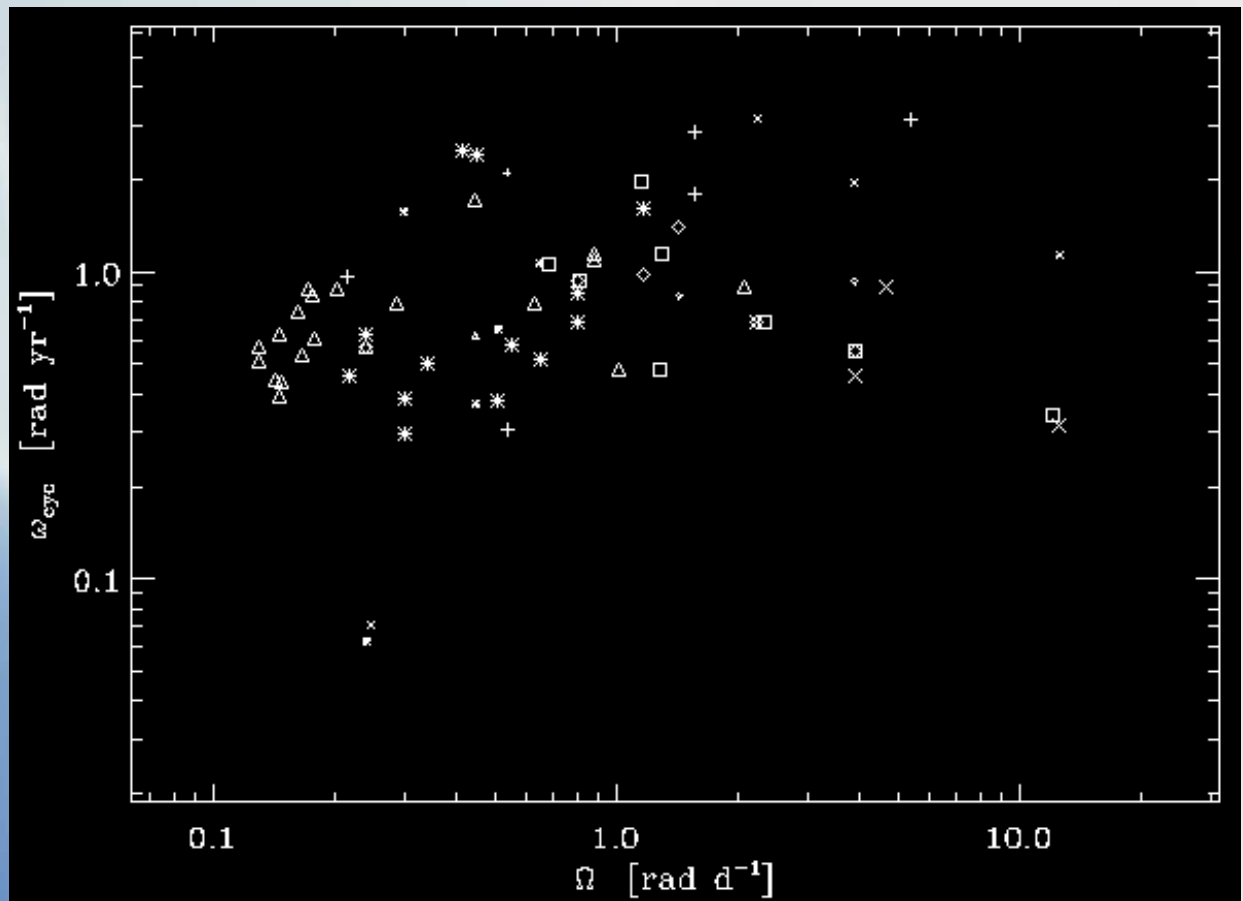
(Work in progress....)

Backtrack from Saar & Brandenburg (1999), take only **single dwarfs**

Update data from with Frick et al (2004), Messina & Guinan (2001), plus....

Nothing obvious at first....

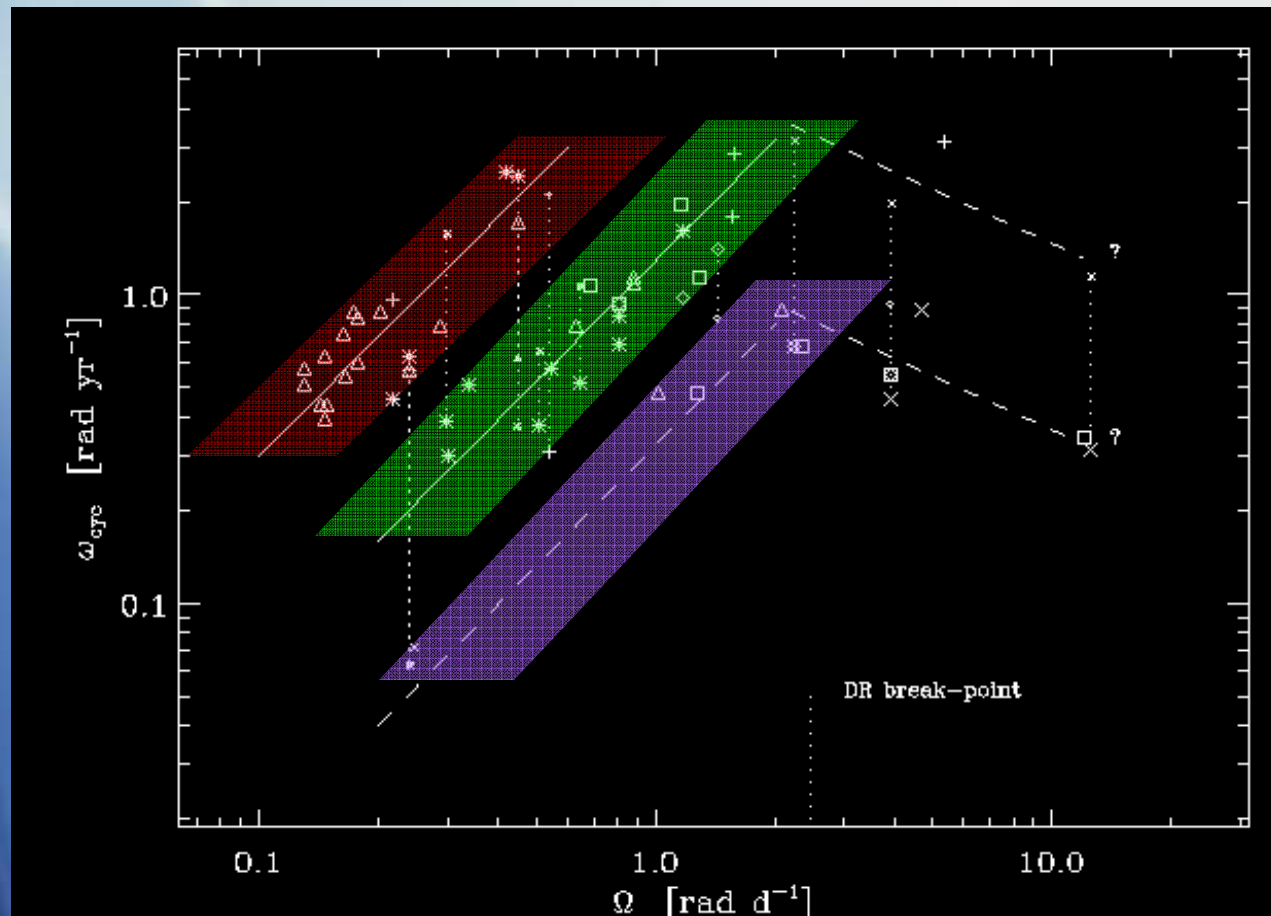
- $\omega_{\text{cyc}} \sim \Omega^{0.0}$  ?
- But consider where secondary  $P_{\text{cyc}}$  (smaller symbols) lie



# Magnetic Cycles II. Cycle Period

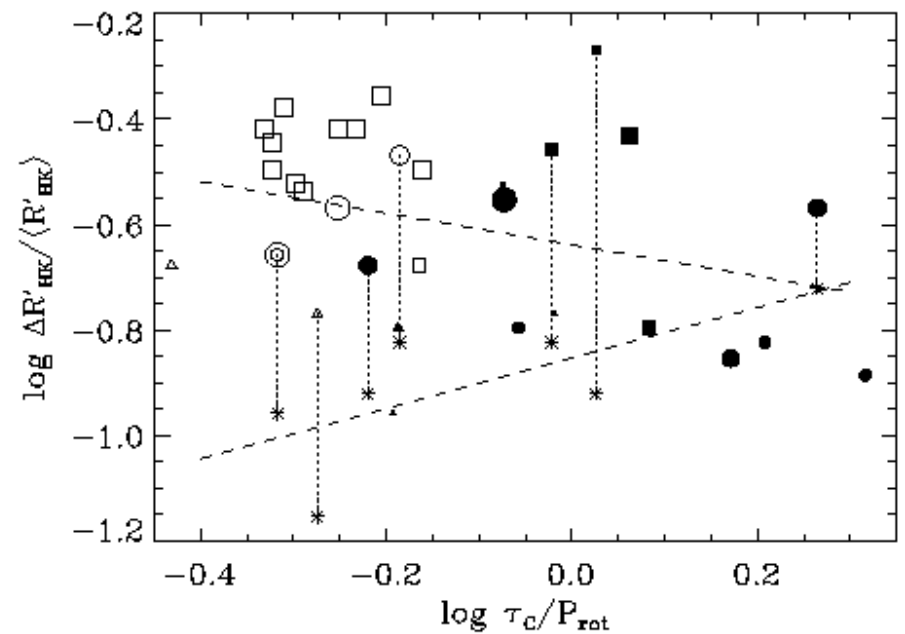
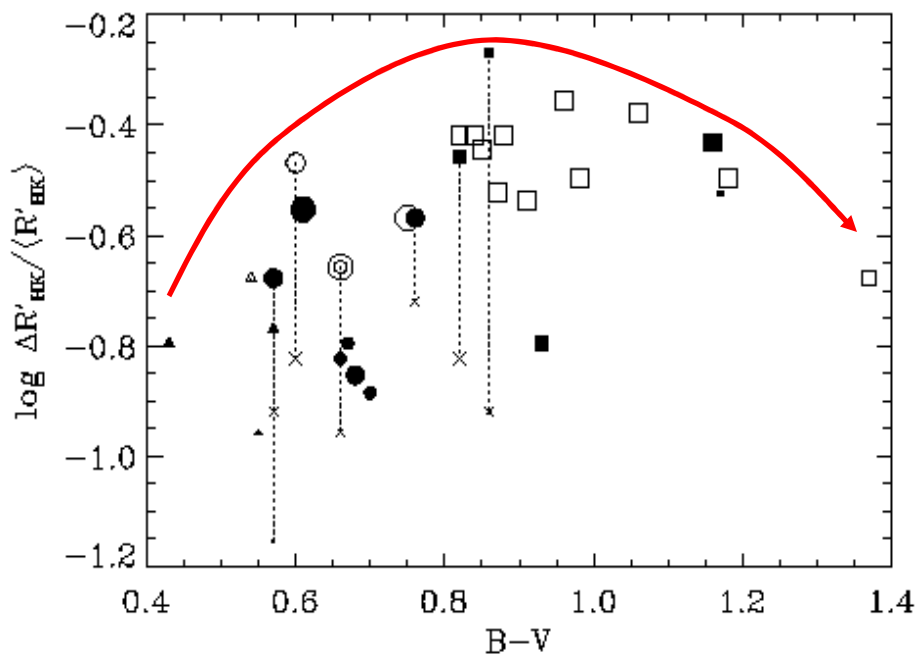
Consider  $P_{\text{cyc}}$  (2nd) (connected to main  $P_{\text{cyc}}$  by vertical dotted)...

- 2 or 3(?) bands, separated by factors of 4, each with  $\omega_{\text{cyc}} \sim \Omega^{1.3}$
- Possible break at  $\Omega \sim 10$  x solar - the **same** point where  $\Delta\Omega$  slope changes....
- Multimode dynamo, with change in behaviour with  $\Delta\Omega$  at high  $\Omega$ ?



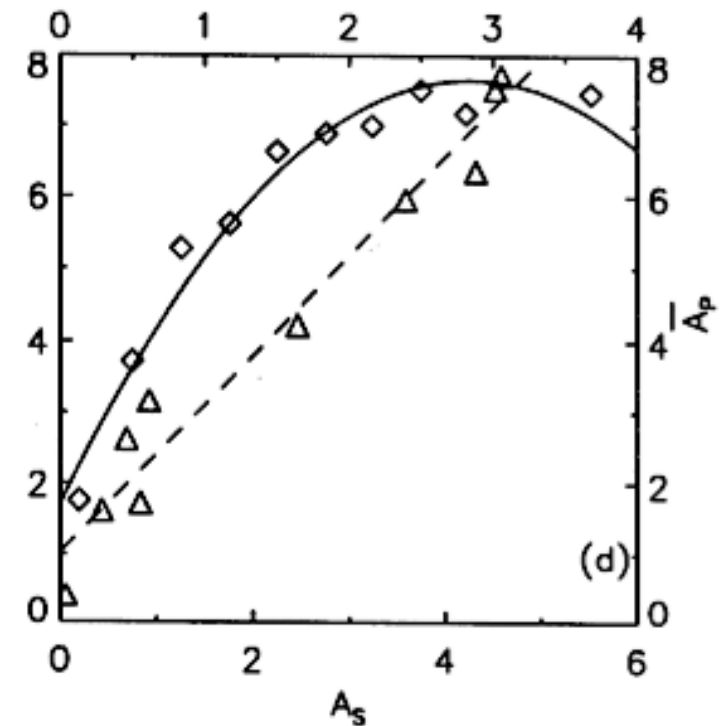
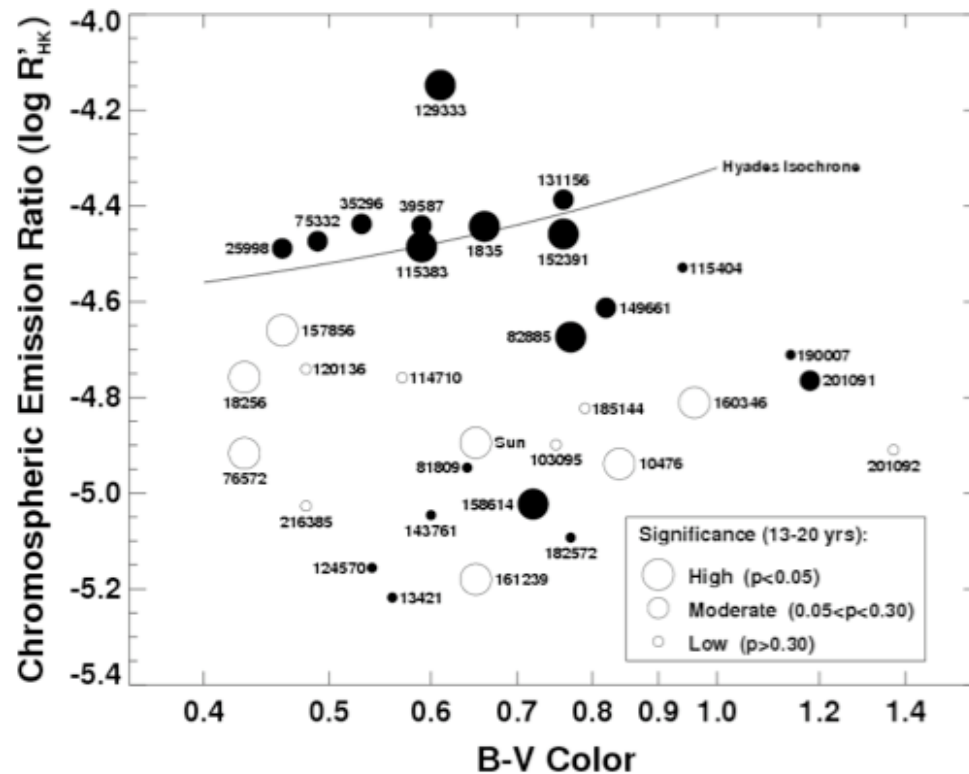
# Magnetic Cycles III. Amplitudes

- Ca II HK = plage/network data: Max  $A_{\text{cyc}}$  increases with B-V to **peak in mid K** (Saar & Brandenburg 2002)  
(recall  $A_{\text{cyc}}$ (spot) kept increasing at low masses)
- $A_{\text{cyc}}$  decreases with  $Ro^{-1}$ ;  $A_{\text{cyc}}$ (2nd) increases with  $Ro^{-1}$  - sign of multimode dynamo? (Moss et al 2008)



# Magnetic Cycles IV. Bright or Dark?

- Look at the sign of the  $A_{\text{HK}} - A_{\text{pho}}$  relation (Radick ea 1998, Lockwood ea 2007)
- Positive for **low  $R'_{\text{HK}}$  stars (vis Sun)** - more activity = brighter  $\Rightarrow$  **plage/network dom.**
- Negative in **high  $R'_{\text{HK}}$  stars** - more activity = fainter  $\Rightarrow$  **spot dominated**  
(Exceptions are either evolved, or low significance)
- Correlation sign change seen in Sun in most active cycles too! (Foukal 1997)



# Long-term variations: minima

The Sun clearly has magnetic Grand minima (and maxima) but their existence in other cool stars has been questioned recently (Wright 2004).

Wright found few low activity ( $\log R'_{\text{HK}} < -5.1$ ) stars within  $\Delta M_V = 1$  of the Main sequence ( $\log M/H = 0$ ). He concluded that truly solar-like stars in Maunder-like minima are rare.

Is the Sun an oddball for having magnetic minima?

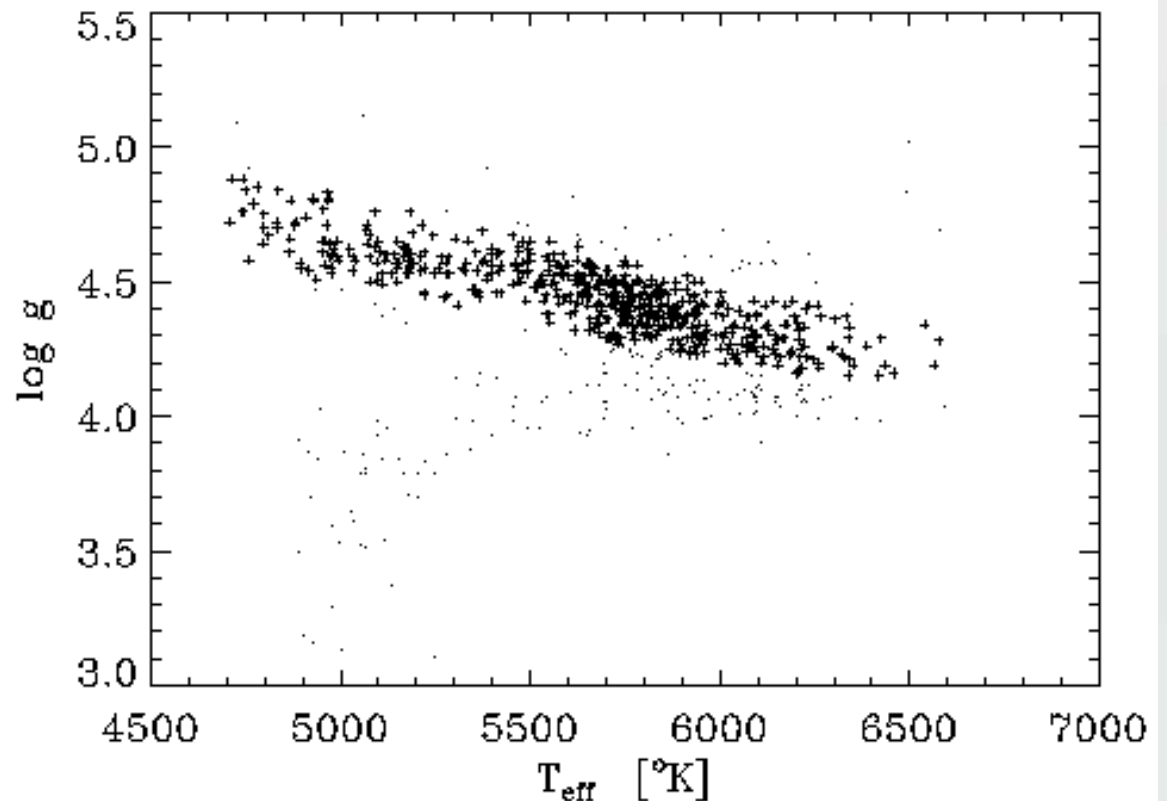
Important for Climate, dynamos, Sun-in-time evolution

**Answer:** yes and no....

# Are Maunder-like minima rare?

Problem: Wright's use of  $\Delta M_V$  confuses evolution and metallicity (M/H) differences. Cleanly separate dwarfs by using spectroscopically determined  $T_{\text{eff}}$  and  $\log g$  values (Valenti & Fischer 2005).

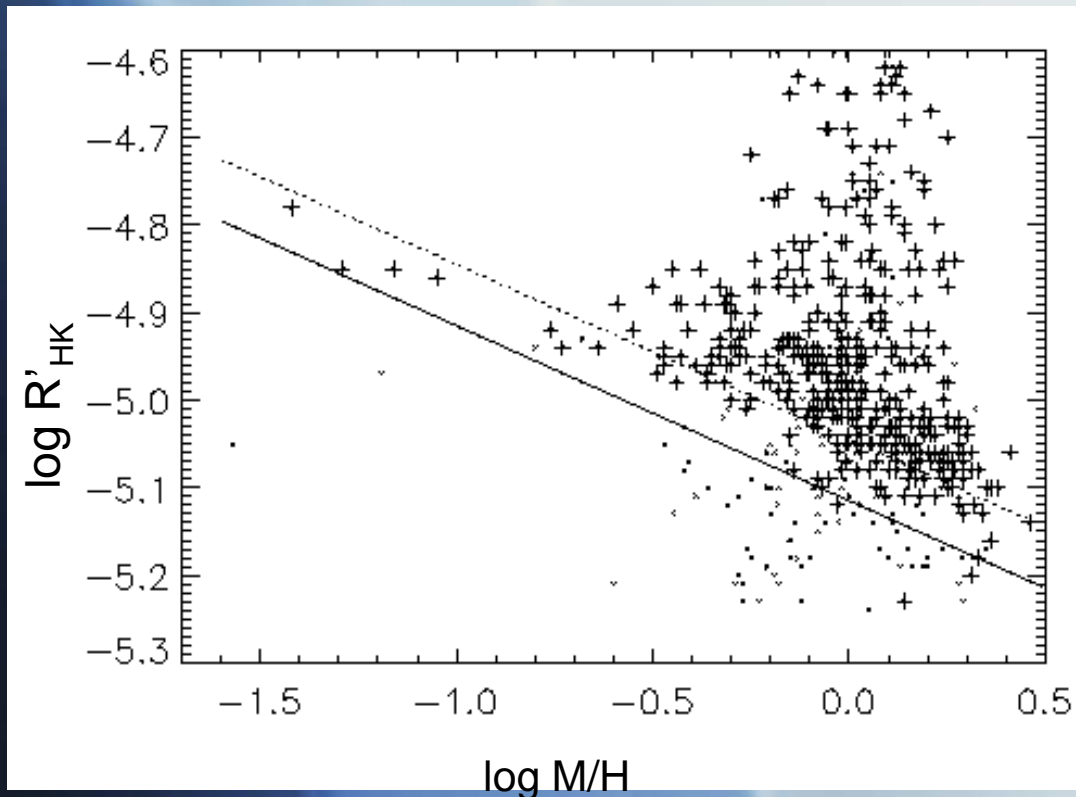
When you do this, dwarfs may be separated independent of their M/H.



# Are Maunder-like minima rare? II

Do this and minimum activity ( $R'_{\text{HK}}$ ) in dwarfs is (apparently) a strongly *decreasing* function of metallicity M/H!

Trend should be flat or even reversed ( $S_{\text{HK}} = C_{\text{core}}/C_{\text{cont}}$ ;  $C_{\text{core}} \sim$  same,  $C_{\text{cont}} \uparrow$  at low M/H)



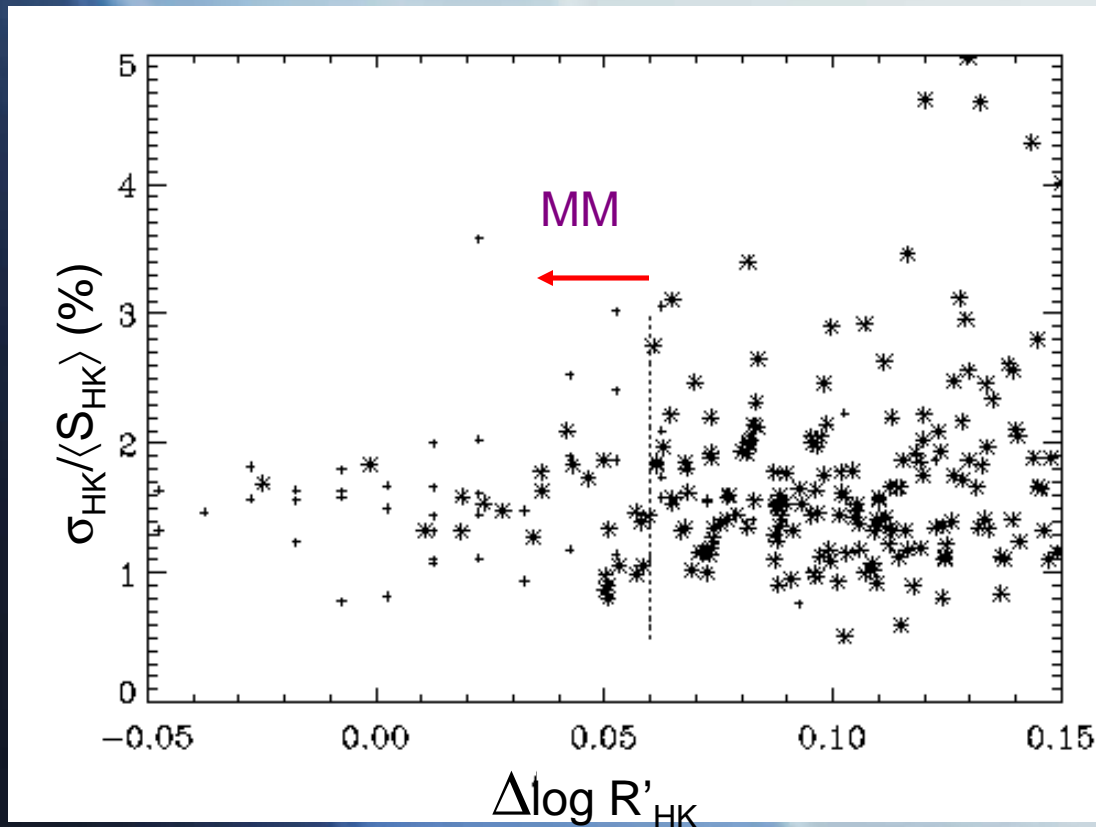
- Likely there is an HK calibration problem
  - Flat  $\log R'_{\text{HK}} < -5.1$  MM level inappropriate
  - Instead, look for MM stars near bottom dwarf  $R'_{\text{HK}}$  boundary
- + = dwarf, x = evolved



# Are Maunder-like minima rare? III

Dwarfs within  $\Delta \log R'_{\text{HK}} \leq 0.06$  ( $\sim +15\%$ ) of  $R'_{\text{HK}}(\text{M}/\text{H})$  boundary show minimal variability ( $\sigma_{\text{HK}}/\langle S_{\text{HK}} \rangle \leq 2\%$ ).

These are our new Maunder minimum star candidates.



- MM candidates:

$$\langle T_{\text{eff}} \rangle = 5730 \pm 271 \text{ K}$$

$$\langle [\text{M}/\text{H}] \rangle = -0.015 \pm 0.400$$

6.1% of sample dwarfs

- Sample:

$$\langle T_{\text{eff}} \rangle = 5610 \pm 379 \text{ K}$$

$$\langle [\text{M}/\text{H}] \rangle = -0.015 \pm 0.228$$

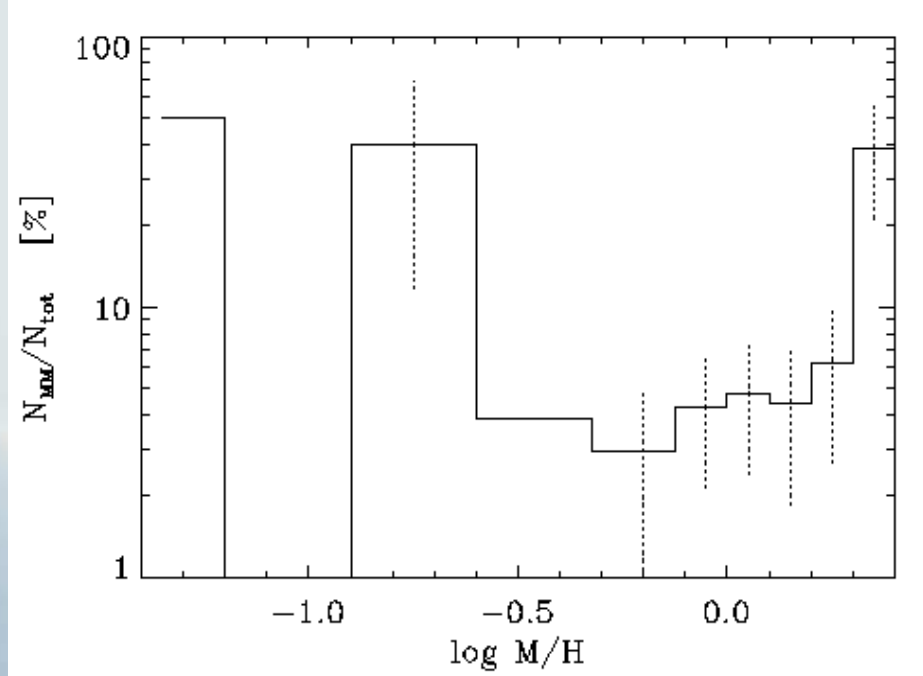
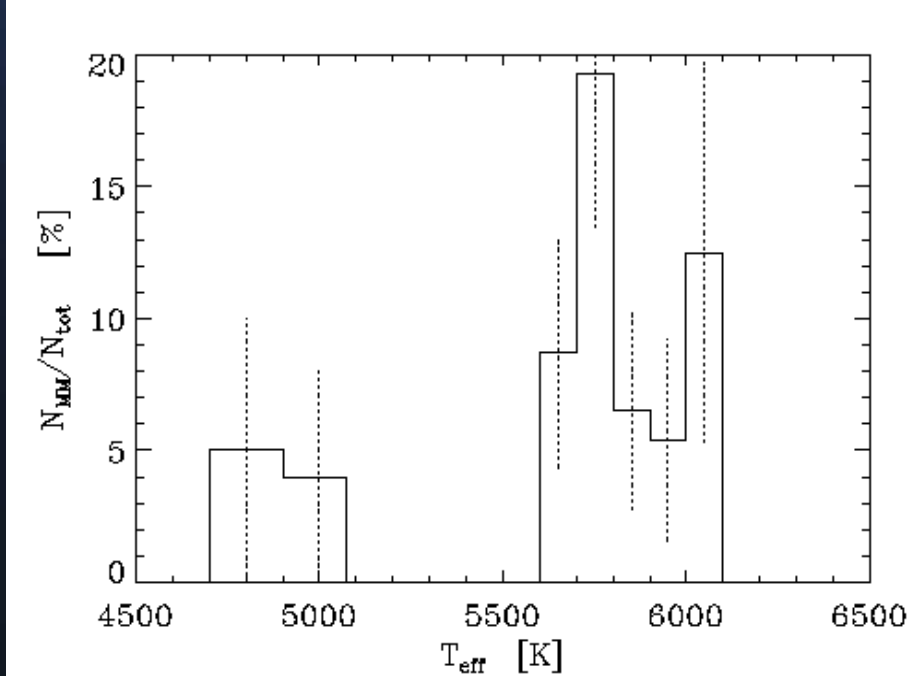
- $\therefore$  MMs have narrower  $T_{\text{eff}}$  but wider M/H distribution

\* = dwarf; + = evolved

# Are Maunder-like minima rare? IV

**Answer(?): No**, ~8% of G dwarfs in sample are MM candidates. But only ~1% of K dwarfs and ~3% of F dwarfs (all F8-9) are candidates.

- Consistent with number of “flat activity” stars in solar-age M67 (Giampapa et al 2006) if binaries excluded.
- No MM candidates in  $T_{\text{eff}}$  gap 5100-5600 K (~K1 to G5), few cooler.
- MM candidates more frequent in low and high metallicities.

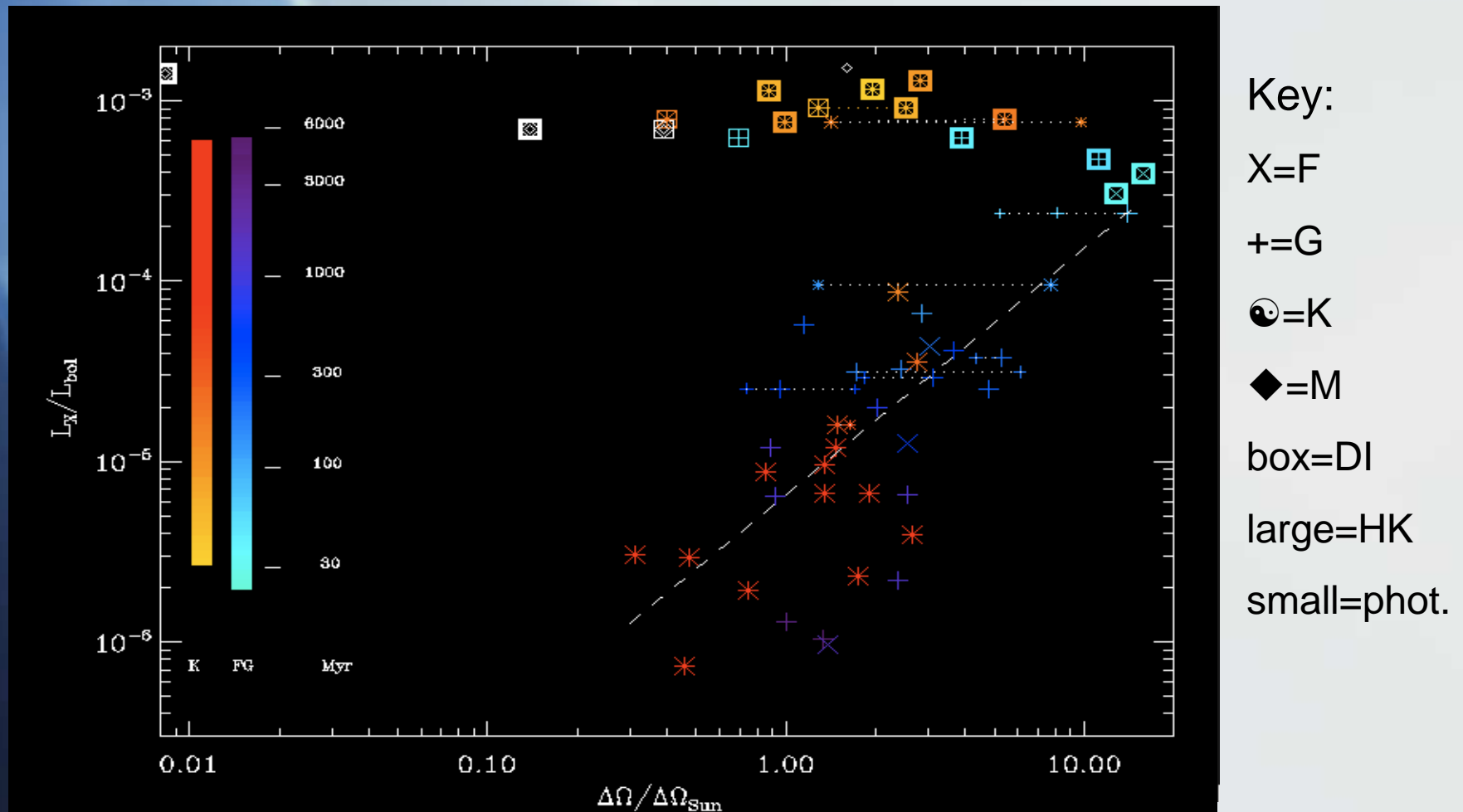


# About the new Maunder-like candidates

- Mostly G5-F9 stars. All metallicities, but low and high M/H favored.
- About 8% of G dwarfs in Wright et al (2004) sample with  $\sigma_{\text{HK}}$  are candidates. Sample is biased to low activity, tho!
- This is consistent with number of “flat activity” stars in solar-age M67 (Giampapa et al 2006) if binaries/outliers excluded.
- None of the MM candidates in the Wright et al sample has been detected in X-rays to date.
- Statistics are meager, but MM candidates in the Wilson cycle sample are consistent with being drawn from the same  $\text{Ro}^{-1}$  (~dynamo number) distribution of non-candidate dwarfs, *if* non-MMs are restricted to ages > 2 Gyr.  $\Rightarrow$  MM candidates are rotationally indistinguishable from older (>2 Gyr), variable dwarfs. They are capable of cycles, but don't have them now.
- Sun is not odd. Possibly all older early-mid G stars have some Maunder-like episodes. Young Sun did not.



# SDR vs. $L_x/L_{bol}$ (proxy for B, dynamo)

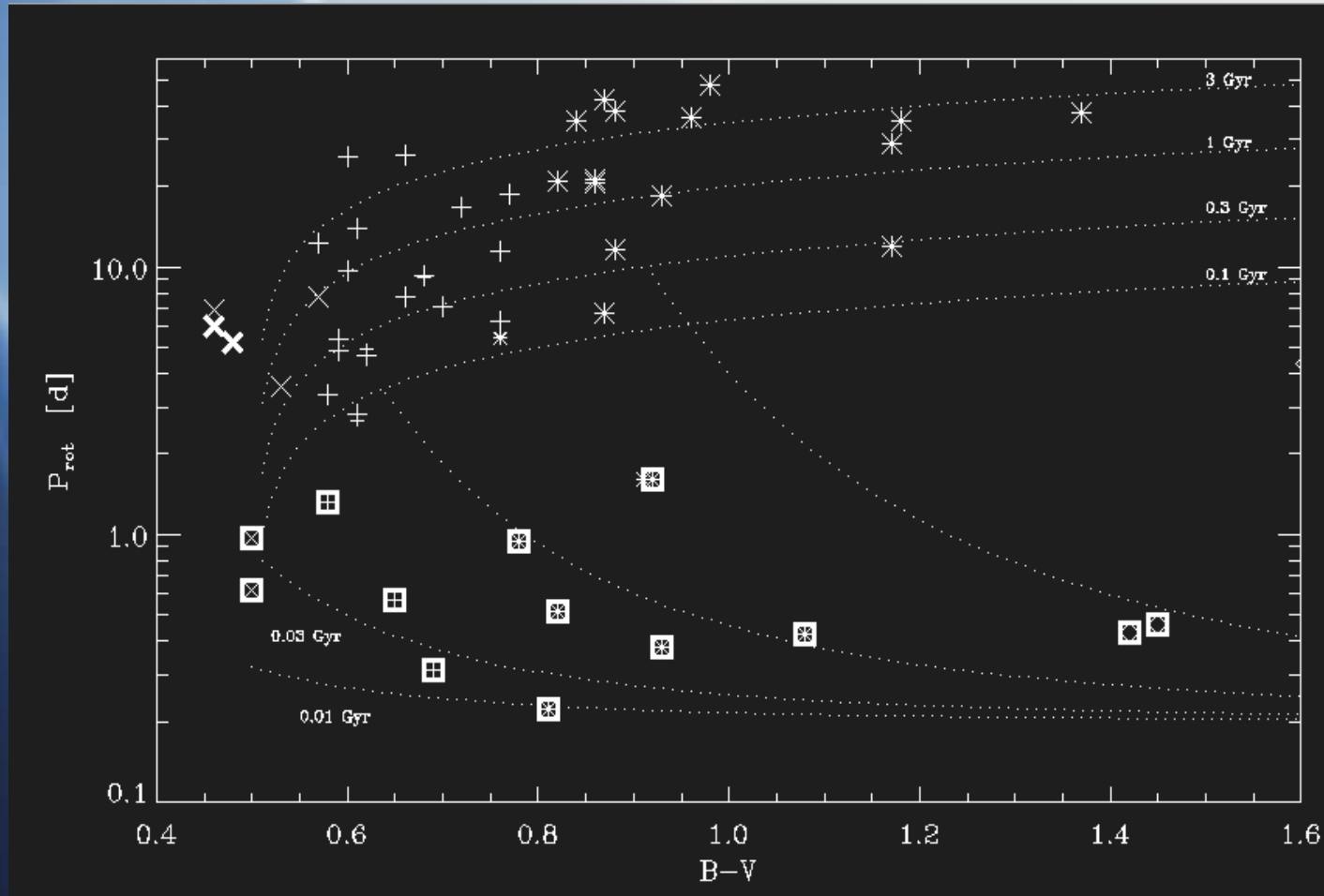


$L_x/L_{bol} \sim \Delta\Omega^{1.36} \quad \sigma = 0.48 \text{ dex for } L_x/L_{bol} < 6 \times 10^{-4} \quad (\Omega < 10 \text{ d}^{-1})$

$L_x/L_{bol} \sim 10^{-3}$  (for  $\Omega > 10 \text{ d}^{-1}$ ), saturation - for all  $\Delta\Omega$  !

⊗  $L_x/L_{bol}$  a maximum regardless of  $\Delta\Omega$  !

# Check color - $P_{\text{rot}}$ diagram

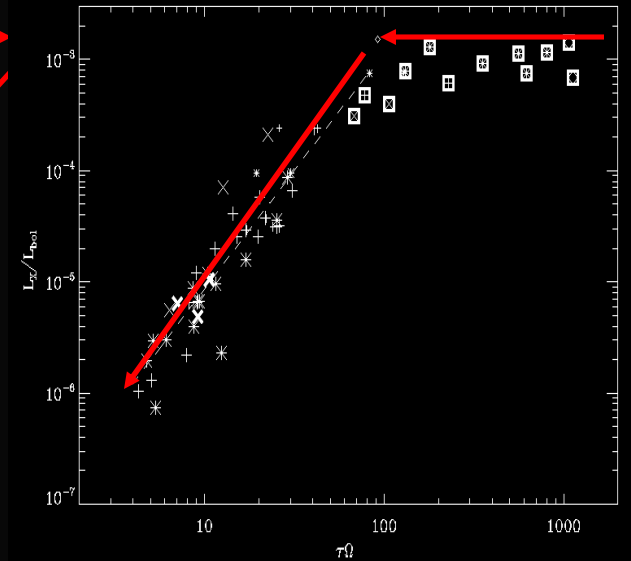
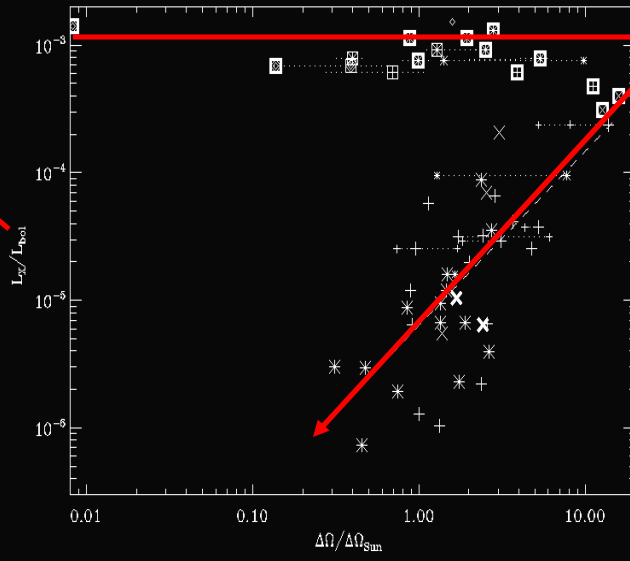
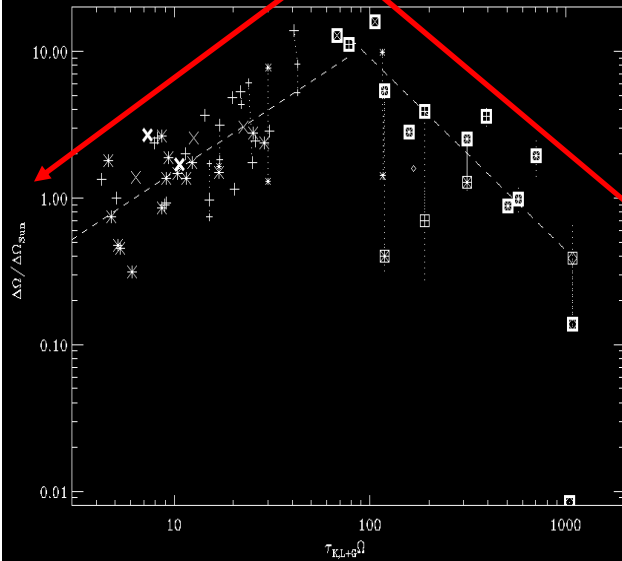


- Key:
- X=F
  - + = G
  - ☯ = K
  - ◆ = M
  - box = DI
  - bold = FTLP
  - large = HK

Stars with increasing/decreasing shear neatly divide into Sydney's I (interface dynamo?)/C (convective dynamo?) branches.

# The Evolution of SDR (combined view)

Arrow of time:  $\longrightarrow$



$\Delta\Omega - Ro$

$L_x/L_{bol} (B) - \Delta\Omega$

$L_x/L_{bol} - Ro$

$\Delta\Omega$  increases to a maximum as  $\Omega$  declines, then decreases.

$L_x/L_{bol}$  is steady during the initial  $\Delta\Omega$  increase, but decays once  $\Delta\Omega$  begins to decrease.

Initially:  $\Delta\Omega \sim Ro^{+1.3}$  while  $L_x/L_{bol} \sim 10^{-3}$  (saturated activity)

Then  $\Delta\Omega \sim Ro^{-0.9}$  after  $Ro^{-1} \sim 80$  or  $\Omega < 10 \text{ d}^{-1}$

# Summary: Two SDR regimes!

- $\Delta\Omega$  increases with  $\Omega$  at low  $\Omega$  (standard rotation-activity, Sydney's I branch - solar-like tachocline/interface dynamo, local  $\tau_c$  best)
- $\Delta\Omega$  decreases with  $\Omega$  at high  $\Omega$  (saturated activity, shear dynamo ineffective, Sydney's C branch - so... convective/turbulent dynamo?, global  $\tau_c$  best)

**Evolutionary scenario:** starting with low  $\Delta\Omega$  and high  $\Omega$  and a convective dynamo, stars spin down gradually increasing  $\Delta\Omega$  at CZ/radiative zone interface until  $\Delta\Omega$  is large enough to “take over” (at  $\sim 60$  Myr in G stars,  $\sim 120$  Myr in early K,  $\sim 1$  Gyr late M). Thereafter, more efficient tachocline dynamo is dominant, and spindown increases; magnetic activity steadily decreases.



# Some implications

Convective dynamo in rapidly rotating stars could explain:

- Low latitude spots (should be high latitude/polar if arising from tachocline dynamo)
- Strong dynamo action in tachocline-less 3D models (Brown et al. 2007)
- Reduced activity changes with  $\Omega$  on saturation branch
- Reduced spindown rate in younger stars
- Gradual convective  $\blacktriangle$  tachocline/ transition could explain lack of activity break in M stars